Assignment \#3, Due 7/31(or 8/1)/2024

1. Distance and Absenteeism. A large city hospital conducted a study to investigate the relationship between the number of unauthorized days that employees are absent per year and the distance (kilometers) between home and work for the employees. A sample of 10 employees was selected and the following data were collected.

| Distance to Work <br> (kilometers) | Number of Days <br> Absent |  |
| :--- | :--- | :--- |
| 1 | 8 |  |
| 3 | 5 |  |
| 4 | 8 |  |
| 6 | 7 |  |
| 8 | 6 |  |
| 10 | 3 |  |
| 12 | 5 |  |
| 14 | 2 |  |
| 14 | 4 |  |
| 18 | 2 |  |

(a) Develop a scatter diagram for these data. Does a linear relationship appear reason- able? Explain.
(b) Develop the least squares estimated regression equation that relates the distance to work to the number of days absent.
(c) Predict the number of days absent for an employee who lives 5 kilometers from the hospital.
2. Go to https://dasl.datadescription.com/ and download the heights and weights of students in a statistics class ("Heights_and_weights"). Then use the variable "Weight" as the dependent variable and "Height" as the independent variable.
(a) Use Excel (or other statistical software) to finish the regression analysis. Then compare your outputs from t-test and ANOVA table, and comment on what you find.
(b) Construct a $99 \%$ confidence interval for the estimate of slope.
(c) Suppose we want to predict the weight of student of heights 60,65 , and 70 inches. Give your prediction values and their prediction intervals.
3. Used Car Mileage and Price. The Toyota Camry is one of the best-selling cars in North America. The cost of a previously owned Camry depends upon many factors,
including the model year, mileage, and condition. To investigate the relationship between the car's mileage and the sales price for a 2007 model year Camry, the following data show the mileage and sale price for 19 sales.
(a) Develop a scatter diagram with the car mileage on the horizontal axis and the price on the vertical axis.
(b) Develop the estimated regression equation that could be used to predict the price ( $\$ 1000$ s) given the kilometers (1000s).
(c) Test for a significant relationship at the .05 level of significance.
(d) Did the estimated regression equation provide a good fit? Provide an interpretation for the slope of the estimated regression equation.
(e) Suppose that you are considering purchasing a previously owned 2007 Camry that has been driven 97,000 kilometers. Using the estimated regression equation developed in part (c), predict the price for this car. Is this the price you would offer the seller?

| Kilometers (1000s) | Price $\mathbf{( \$ 1 0 0 0 s})$ |
| :---: | :---: |
| 35 | 16.2 |
| 47 | 16.0 |
| 58 | 13.8 |
| 76 | 11.5 |
| 101 | 12.5 |
| 124 | 12.9 |
| 117 | 11.2 |
| 140 | 13.0 |
| 148 | 11.8 |
| 163 | 10.8 |
| 177 | 8.3 |
| 45 | 12.5 |
| 95 | 11.1 |
| 109 | 15.0 |
| 109 | 12.2 |
| 146 | 13.0 |
| 68 | 15.6 |
| 105 | 12.7 |
| 177 | 8.3 |

4. Scoring Cruise Ships. The Condé Nast Traveler Gold List provides ratings for the top 20 small cruise ships. The data shown below are the scores each ship received based upon the results from Condé Nast Traveler's annual Readers' Choice Survey. Each score represents the percentage of respondents who rated a ship as excellent or very good on several criteria, including Shore Excursions and Food/Dining. An
overall score was also reported and used to rank the ships. The highest ranked ship, the Seabourn Odyssey, has an overall score of 94.4, the highest component of which is 97.8 for Food/Dining.
(a) Determine an estimated regression equation that can be used to predict the over- all score given the score for Shore Excursions.
(b) Consider the addition of the independent variable Food/Dining. Develop the estim- ated regression equation that can be used to predict the overall score given the scores for Shore Excursions and Food/Dining.
(c) Predict the overall score for a cruise ship with a Shore Excursions score of 80 and a Food/Dining Score of 90 .

| Ship | Overall | Shore <br> Excursions | Food/Dining |
| :--- | :---: | :---: | :---: |
| Seabourn Odyssey | 94.4 | 90.9 | 97.8 |
| Seabourn Pride | 93.0 | 84.2 | 96.7 |
| National Geographic Endeavor | 92.9 | 100.0 | 88.5 |
| Seabourn Sojourn | 91.3 | 94.8 | 97.1 |
| Paul Gauguin | 90.5 | 87.9 | 91.2 |
| Seabourn Legend | 90.3 | 82.1 | 98.8 |
| Seabourn Spirit | 90.2 | 86.3 | 92.0 |
| Silver Explorer | 89.9 | 92.6 | 88.9 |
| Silver Spirit | 89.4 | 85.9 | 90.8 |
| Seven Seas Navigator | 89.2 | 83.3 | 90.5 |
| Silver Whisperer | 89.2 | 82.0 | 88.6 |
| National Geographic Explorer | 89.1 | 93.1 | 89.7 |
| Silver Cloud | 88.7 | 78.3 | 91.3 |
| Celebrity Xpedition | 87.2 | 91.7 | 73.6 |
| Silver Shadow | 87.2 | 75.0 | 89.7 |
| Silver Wind | 86.6 | 78.1 | 91.6 |
| SeaDream II | 86.2 | 77.4 | 90.9 |
| Wind Star | 86.1 | 76.5 | 91.5 |
| Wind Surf | 86.1 | 72.3 | 89.3 |
| Wind Spirit | 85.2 | 77.4 | 91.9 |
|  |  |  |  |

5. Use the variable selection commands of regression analysis in Minitab for the following data, e.g. stepwise and best subset regression. (Note: See the following outputs for reference.) Compare their differences and give your comments.
```
y: Total heat flux (kwatts)
x1: Insolation(watts/m2)
x2: Position of focal point in east direction (inches)
x3: Position of focal point in south direction (inches)
x4: Position of focal point in north direction (inches)
x5: Time of day
```

| y x 1 | x2 | x3 | x4 | x5 |
| :---: | :---: | :---: | :---: | :---: |
| 271.8783 .35 | 33.53 | 40.55 | 16.66 | 13.2 |
| 264748.45 | 36.5 | 36.19 | 16.46 | 14.11 |
| 238.8684 .45 | 34.66 | 37.34 | 17.66 | 15.68 |
| 230.7827 .8 | 33.13 | 32.52 | 17.5 | 10.53 |
| 254.6860 .45 | 35.75 | 33.71 | 16.4 | 11 |
| 257.9875 .15 | 34.46 | 34.14 | 16.28 | 11.31 |
| 263.9909 .45 | 34.6 | 34.85 | 16.06 | 11.96 |
| 266.5905 .55 | 35.38 | 35.89 | 15.93 | 12.58 |
| 229.1756 | 35.85 | 33.53 | 16.6 | 10.66 |
| 239.3769 .35 | 35.68 | 33.79 | 16.41 | 10.85 |
| 258793.5 | 35.35 | 34.72 | 16.17 | 11.41 |
| 257.6801 .65 | 35.04 | 35.22 | 15.92 | 11.91 |
| 267.3819 .65 | 34.07 | 36.5 | 16.04 | 12.85 |
| 267 808.55 | 32.2 | 37.6 | 16.19 | 13.58 |
| 259.6774 .95 | 34.32 | 37.89 | 16.62 | 14.21 |
| 240.4711 .85 | 31.08 | 37.71 | 17.37 | 15.56 |
| 227.2694 .85 | 35.73 | 37 | 18.12 | 15.83 |
| 196638.1 | 34.11 | 36.76 | 18.53 | 16.41 |
| 278.7774 .55 | 34.78 | 34.62 | 15.54 | 13.1 |
| 272.3757 .9 | 35.77 | 35.4 | 15.7 | 13.63 |
| 268.4753 .35 | 36.44 | 35.96 | 16.45 | 14.51 |
| 254.5704 .7 | 37.82 | 36.26 | 17.62 | 15.38 |
| 224.7666 .8 | 35.07 | 36.34 | 18.12 | 16.1 |
| 181.5568 .55 | 35.26 | 35.9 | 19.05 | 16.73 |
| 227.5653 .1 | 35.56 | 31.84 | 16.51 | 10.58 |
| 253.6704 .05 | 35.73 | 33.16 | 16.02 | 11.28 |
| 263709.6 | 36.46 | 33.83 | 15.89 | 11.91 |
| 265.8726 .9 | 36.26 | 34.89 | 15.83 | 12.65 |
| 263.8697 .15 | 37.2 | 36.27 | 16.71 | 14.06 |

- Output of Stepwise Regression:
Response is HeatFlux on 5 predictors, with $N=29$

| Step | 1 | 2 | 3 | 4 |
| :---: | :---: | :---: | :---: | :---: |
| Constant | 607.1 | 483.7 | 389.2 | 270.2 |
| North | -21.4 | -24.2 | -24.1 | -21.1 |
| T-Value | -8.34 | -12.48 | -12.92 | -8.91 |
| P-Value | 0.000 | 0.000 | 0.000 | 0.000 |
| South |  | 4.80 | 5.32 | 5.34 |
| T-Value |  | 5.04 | 5.52 | 5.83 |
| P-Value |  | 0.000 | 0.000 | 0.000 |
| East |  |  | 2.1 | 3.0 |
| T-Value |  |  | 1.75 | 2.40 |
| P-Value |  |  | 0.092 | 0.025 |
| Insolation |  |  |  | 0.052 |
| T-Value |  |  |  | 1.92 |
| P-Value |  |  |  | 0.067 |
| S | 12.3 | 8.93 | 8. 60 | 8.17 |
| R-Sq | 72.05 | 85.87 | 87.41 | 89.09 |
| R-Sq(adj) | 71.02 | 84.78 | 85.90 | 87.27 |
| Mallows CP | 38.5 | 9.1 | 7.6 | 5.8 |

- Output of Best Subset Regression:


## Best Subsets Regression: HeatFlux versus Insolation, East, ...

```
Response is HeatFlux
```

|  |  |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
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|  |  |  |  |  |  |  |  |  |
|  |  |  |  |  |  |  | S | N |
|  |  |  |  |  |  | E | - | $\bigcirc \mathrm{I}$ |
|  |  |  |  |  |  | a | u | $r i$ |
|  |  |  | Mallows |  |  | 3 | $t$ | $t \mathrm{~m}$ |
| Vars | R-Sq | R-Sq (adj) | Cp | 5 |  | t | h | $\mathrm{h} e$ |
| 1 | 72.1 | 71.0 | 38.5 | 12.328 |  |  |  | X |
| 1 | 39.4 | 37.1 | 112.7 | 18.154 |  |  |  |  |
| 2 | 85.9 | 84.8 | 9.1 | 8.9321 |  |  | X | X |
| 2 | 82.0 | 80.6 | 17.8 | 10.076 |  |  |  | X X |
| 3 | 87.4 | 85.9 | 7.6 | 8.5978 |  | X | X | X |
| 3 | 86.5 | 84.9 | 9.7 | 8.9110 | X |  | X | X |
| 4 | 89.1 | 87.3 | 5.8 | 8.1698 | X | X | X | X |
| 4 | 88.0 | 86.0 | 8.2 | 8.5550 |  |  | X | X X |
| 5 | 89.9 | 87.7 | 6.0 | 8.0390 | X | X | X | X X |

